## Subtle Authenticated Encryption

Guy Barwell Martijn Stam Daniel Page

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Now with closed-caption sub-titles! Thanks to Eve for scribing an early version of this talk.

Authentication

Authentication

Encryption

Authentication

Authenticated Encryption

Encryption

Authentication

Authenticated Encryption

Encryption

Probabilistic

Deterministic

Authentication

Authenticated Encryption

Encryption

Probabilistic

Deterministic acuoN acue

Authentication

Authenticated Encryption

Probabilistic

Encryption

Deterministic IV based

Probabilistic

Authentication

Authenticated Encryption

Encryption

Deterministic Nonce

Nonce-based but actually mean random-IV based

IV based

Probabilistic

Authentication

Authenticated Encryption

Encryption

## Deterministic Nonce

Nonce-based but actually mean random-IV based

IV based

#### Probabilistic **Stateless**

Authentication

Authenticated Encryption

Encryption

Deterministic

Nonce

Nonce-based but actually mean random-IV based

⊃ Stateful Probabilistic Stateless Authentication

Authenticated Encryption

Encryption

Nonce<br/>Nonce-based but actually<br/>mean random-IV basedAuthenticated<br/>EncryptionIV based<br/>StatefulStatefulProbabilisticStateless

IND-CPA

Oh look, now he's got them flying in – that explains why this wasn't in Beamer.

# NonceAuthenticationAuthenticated<br/>EncryptionNonce-based but actually<br/>mean random-IV basedINT-CTXTINT-CTXTIV based<br/>StatefulStatefulEncryptionProbabilisticStatelessStateless

IND-CPA

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, Determi			INT-C	TXT INDS	S-CCA3	Semantic	
			RAE	En	cryption	n NDĆ	
Pr	obabilistic	Statel	ess	priv		ΠΝΟŞ	
RUP			Distinguishable Decryptions	IND-CPA	LOR IND-CCA		
					IND-CCA		

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с		Ei-Ei-Oh Sec	cure				Post-Quantum	
nisti	Nonce	(Old McDonald mo	Aut	nentication		Aut Enc	Authenticated Encryption	
ermi	Nonce-based but actually mean random-IV based		INT-CTXT Secure for all adversaries making $q \le 2^{-n}$ queries RAE				Semantic	
Dete	IV based Stateful				Encryption			
Probabilistic Statel		<b>ess</b>	Kid-brother-pro <b>p</b>		IND	\$		
	RUP		Distinguishable		priv	LOR	its probably secure	
One-way passive secu		Decryptions rity	IND-(	CPA	IND-CCA			

May contain traces of nuts

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#### There are too many different formalisations!

"Too many formalisations" – He's blatantly going to show that old XKCD cartoon...

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"Too many formalisations" – He's blatantly going to show that old XKCD cartoon Told you! That's not at all derivative...

$$\begin{array}{rcl} \mathrm{Enc}, \mathcal{E} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{M} & \to & \mathsf{C} \\ \mathrm{Dec}, \mathcal{D} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \mathsf{M} & \cup & \{\bot\} \\ & \Lambda & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \{\top\} & \cup & \mathsf{L} \end{array}$$

Definitional choices:

• Nonce Based (deterministic)

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Definitional choices:

- Nonce Based (deterministic)
- Tidy & Correct

We require schemes be nonce-based, correct and tidy. This means the scheme is wholly specified by  $\mathcal{E}$ , and the implementation leakage by  $\Lambda$ 

$$\begin{array}{rcl} \mathrm{Enc}, \mathcal{E} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{M} & \to & \mathsf{C} \\ \mathrm{Dec}, \mathcal{D} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \mathsf{M} & \cup & \{\bot\} \\ & \Lambda & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \{\top\} & \cup & \mathsf{L} \end{array}$$

Definitional choices:

- Nonce Based (deterministic)
- Tidy & Correct
- Real World vs Ideal World

$$\begin{array}{rcl} \mathrm{Enc}, \mathcal{E} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{M} & \to & \mathsf{C} \\ \mathrm{Dec}, \mathcal{D} & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \mathsf{M} & \cup & \{\bot\} \\ & \Lambda & : \mathsf{K} \times \mathsf{N} \times \mathsf{A} \times \mathsf{C} & \to & \{\top\} & \cup & \mathsf{L} \end{array}$$

Definitional choices:

- Nonce Based (deterministic)
- Tidy & Correct
- Real World vs Ideal World
- Separate out Leakage from D

#### Oracles look like this:



The adversary is provided with some subset of these 5 oracles, and tasked with distinguishing which world the challenge oracles are taken from.

#### And interact like this:



Key:

- Prohibited Queries
- --> Pointless Queries
- Entangled Oracles

An arrow  $A \rightarrow B$  means that queries made to A restrict queries to B. Arrows within the same row mean inputs cannot be repeated, those from one row to another mean the output of A cannot later be used as input to B.

There are a large number of queries that must be forbidden to prevent trivial wins, and several others that are pointless.

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There are a large number of queries that must be forbidden to prevent trivial wins, and several others that are pointless. Blah blah, formal stuffs - this is getting a bit dull isn't it? Tell you what, I'll add a funny picture before the next slide... "The trouble with quotes on the Internet is that you can never know if they are genuine."

Abraham Lincoln



Source: https://goo.gl/JHs7QL

You're welcome

#### We define security games like this:



Schemes are named in such a way that reflects clearly which oracles the adversary has access to. This leads to lots of games, but luckily many of them are equivalent

#### Which are related like this:



The same relations between the subtle cases, which are completely separated from the leakage-free case

#### We also introduce Error Invariance:



Inspired by the INV-ERR notion of BDPS and the DI notion of RUP, we introduce Error Invariance, or ERR—, to measure "how bad" errors are. It can be paired with any 'power' oracles: Guy has drawn ERR—CCA.

#### We also introduce Error Invariance:



Note use of a separately drawn key rather than a different simulator: a scheme is fully specified by ( $\mathcal{E}$ ,  $\Lambda$ )



## Dog + Wig U Terrified Postman

Sorry about that, got a bit heavy – have another fun picture (source <a href="http://imgur.com/gallery/ouO6lj4">http://imgur.com/gallery/ouO6lj4</a> )



The cube above "acts nicely". So, the composition results implied hold, giving us useful decompositions for SAE and AE



Finally then, a decent a decent Tikz image, although it's a bit blurry in these slides.



Finally then, a decent a decent Tikz image, although it's a bit blurry in these slides. Presumably the full paper has a nice vector version though, probably worth a look...



Thank you for your time.

http://eprint.iacr.org/2015/895